

Emittance grown by gas in hybrid channel (preliminary)

K. Yonehara
APC, Fermilab

Overview

- Estimate heating of muon beam due to interaction with buffer gas in a hybrid channel
 - Buffer gas consists either pure gaseous hydrogen or SF6 doped GH2
- For simplicity, I assume no energy loss process
 - Momentum is constant in a channel

Heating model

- Conventional equilibrium emittance formula

$$\varepsilon_{t,n} \propto \frac{\bar{\beta}_t}{X} \quad \bar{\beta}_t : \text{Average transverse beta function}$$

- Formula for a radiation length

$$\frac{1}{X} = \sum_i \frac{w_i}{X_i} \quad w_i: \text{Statistic weight}$$

where I used

$$\rho_{\text{H}_2} = 8.89\text{e-}5 \text{ g/cm}^3, X_{\text{H}_2} = 63.04 \text{ cm}^2/\text{g}$$

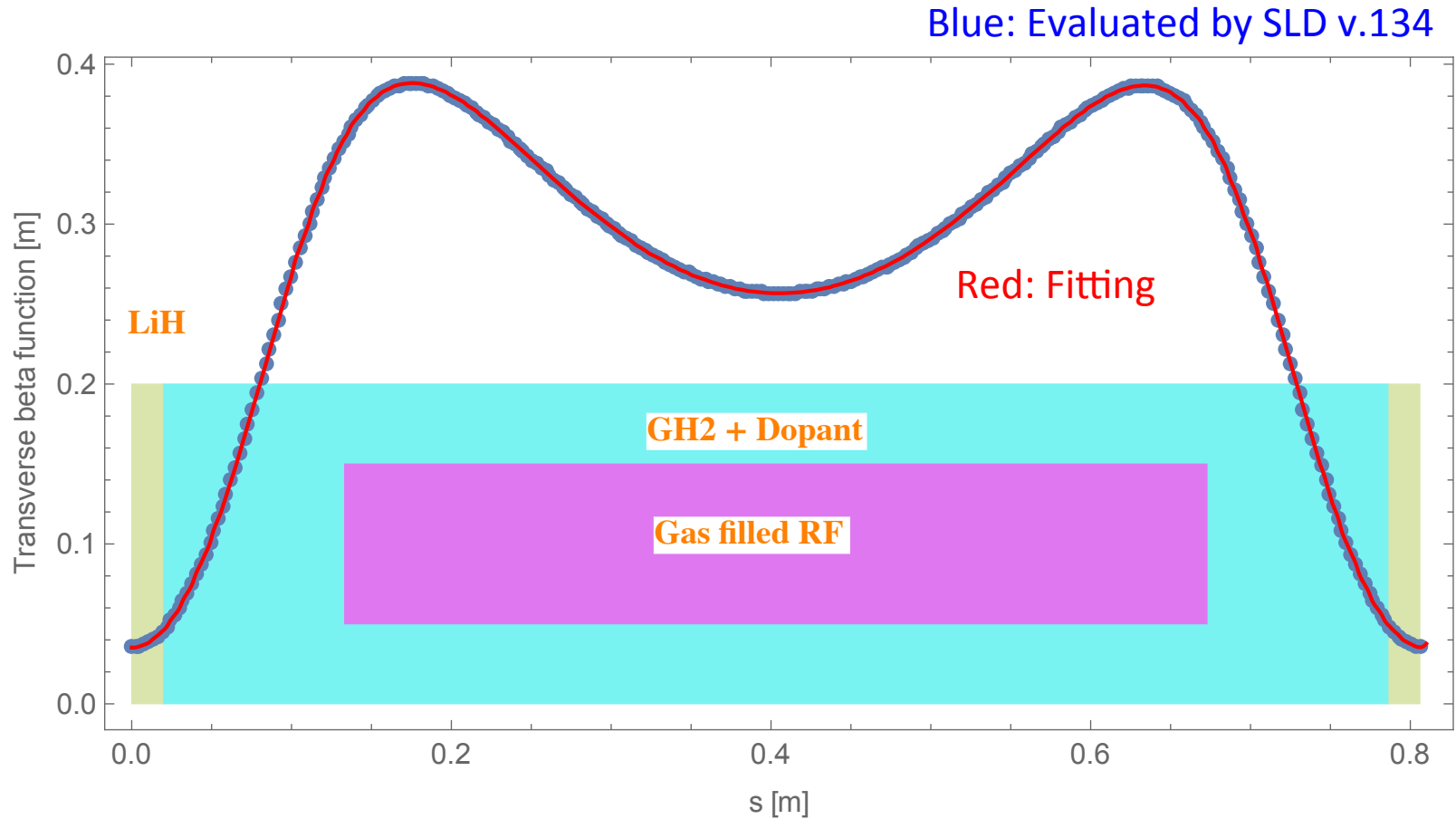
$$\rho_{\text{S}} = 1.43\text{e-}3 \text{ g/cm}^3, X_{\text{S}} = 19.50 \text{ cm}^2/\text{g}$$

$$\rho_{\text{F}} = 1.58\text{e-}3 \text{ g/cm}^3, X_{\text{F}} = 32.93 \text{ cm}^2/\text{g}$$

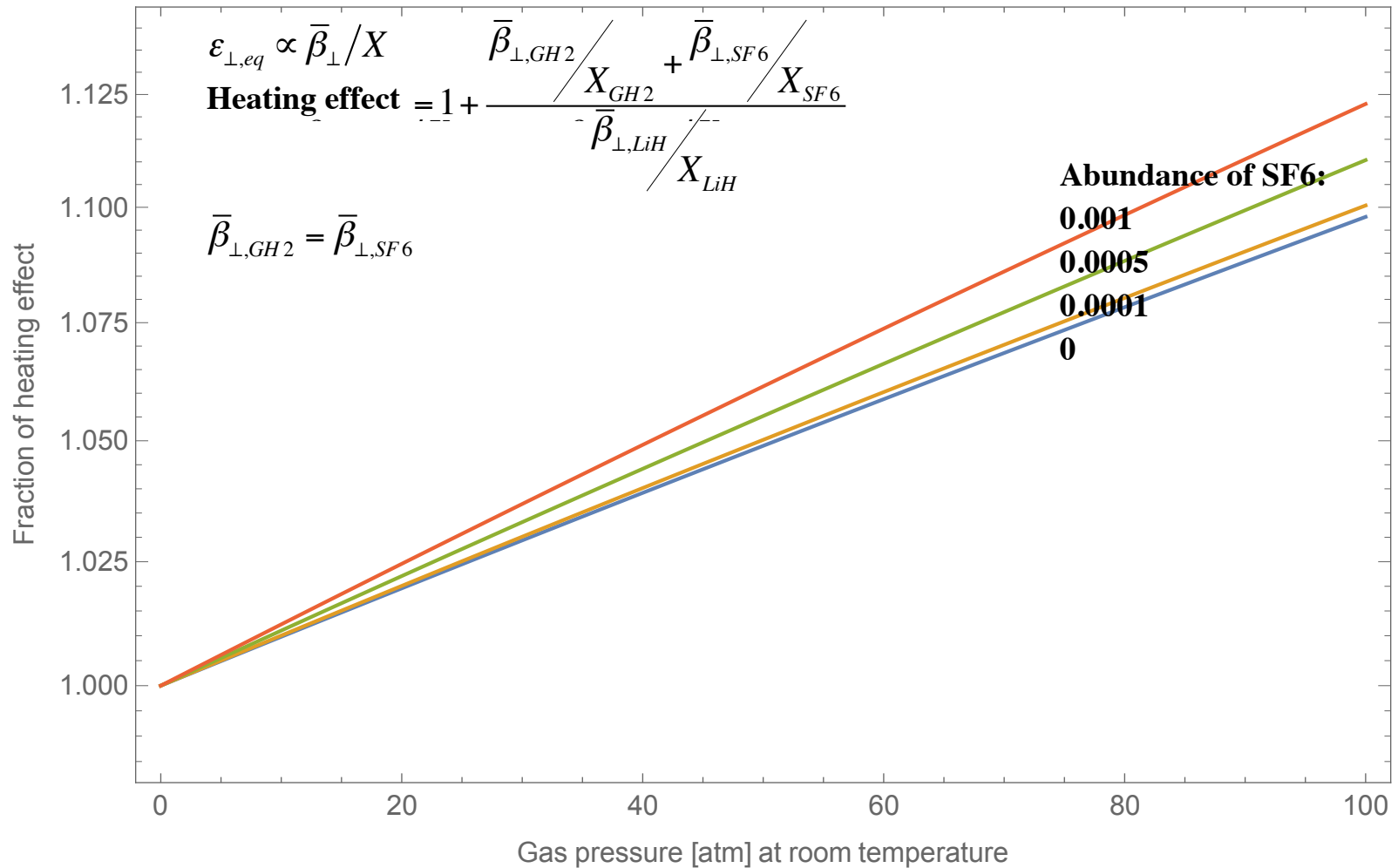
$$\rho_{\text{LiH}} = 0.82 \text{ g/cm}^3, X_{\text{LiH}} = 79.62 \text{ cm}^2/\text{g}$$

from PDG

Transverse beta function in a rectilinear channel

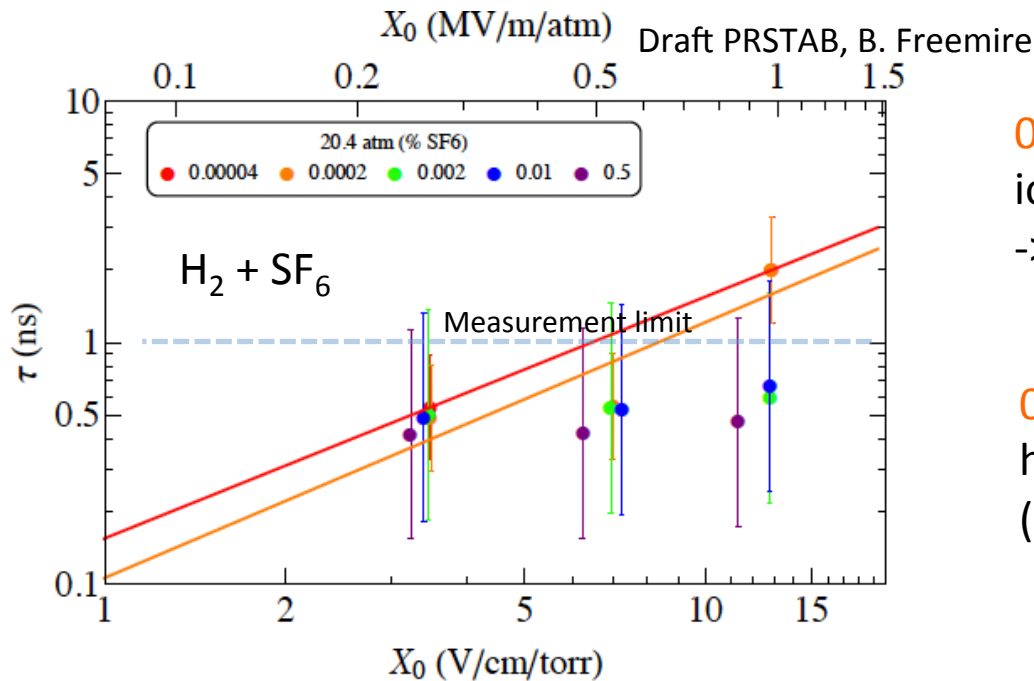


Estimate heating effect



Electron capture in SF6

Observed electron capture constant in HPRF test



0.0002 of SF6 is sufficient to capture ionization electrons in 1 ns
→ Plasma loading is manageable

0.0002 of SF6 in 100 atm GH2 will heat the muon beam by only 10 %
(see the plot in previous slide)

$X_0 \sim 4$ V/cm/torr for $E = 30$ MV/m in $P = 100$ atm

Discussion

- Emittance grown by buffer gas is small
 - 80 ~ 100 atm looks acceptable
 - A small fraction of SF₆ dopant significantly reduces the plasma loading effect
 - Heating by a buffer gas will be comparable with the heating by Be RF windows
 - I need to know the exact location of windows and their geometries to estimate the window effect
- Need to re-evaluate cooling simulation
 - Energy loss along the beam path will make lower beta function, i.e. gas may provide lower equilibrium emittance